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Centre number

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Candidate number

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Surname

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Candidate signature

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I declare this is my own work.

# A-level MATHEMATICS

## Paper 1

Tuesday 4 June 2024

Afternoon

Time allowed: 2 hours

### Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
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<b>TOTAL</b>	



J U N 2 4 7 3 5 7 1 0 1

G/LM/Jun24/G4005/E6

**7357/1**

Answer **all** questions in the spaces provided.

- 1** Find the coefficient of  $x$  in the expansion of

$$(4x^3 - 5x^2 + 3x - 2)(x^5 + 4x + 1)$$

Circle your answer.

**[1 mark]**

-5

-2

7

11



2 The function  $f$  is defined by  $f(x) = e^x + 1$  for  $x \in \mathbb{R}$

Find an expression for  $f^{-1}(x)$

Tick (✓) **one** box.

[1 mark]

$f^{-1}(x) = \ln(x - 1)$

$f^{-1}(x) = \ln(x) - 1$

$f^{-1}(x) = \frac{1}{e^x + 1}$

$f^{-1}(x) = \frac{x - 1}{e}$

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3 The expression

$$\frac{12x^2 + 3x + 7}{3x - 5}$$

can be written as

$$Ax + B + \frac{C}{3x - 5}$$

State the value of  $A$

Circle your answer.

[1 mark]

3

4

7

9

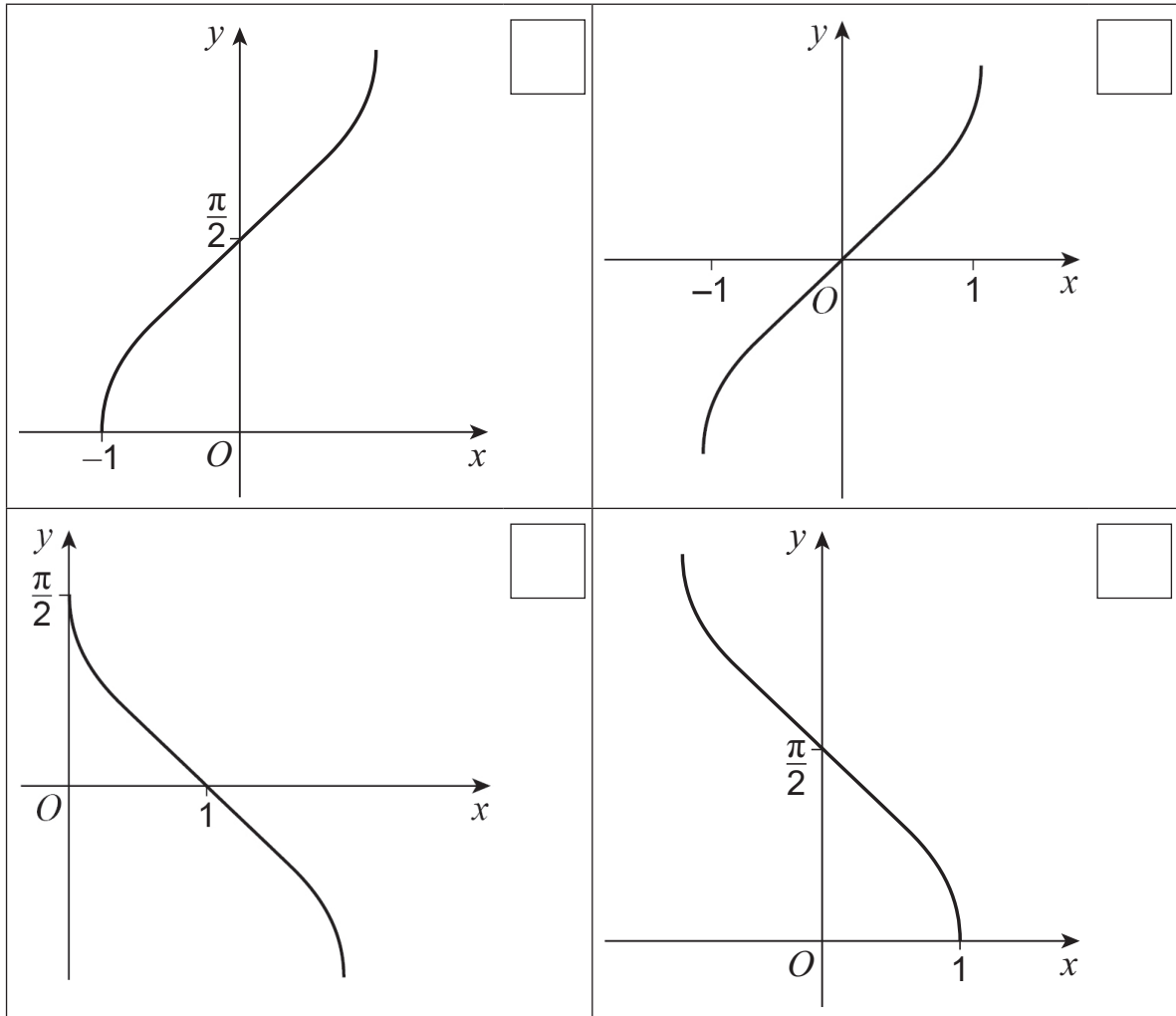


4 One of the diagrams below shows the graph of  $y = \arccos x$

Identify the graph of  $y = \arccos x$

Tick (✓) **one** box.

[1 mark]



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- 8 (a)** Find the first three terms, in ascending powers of  $x$ , in the expansion of

$$(2 + kx)^5$$

where  $k$  is a positive constant.

**[3 marks]**

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- 8 (b)** Hence, given that the coefficient of  $x$  is four times the coefficient of  $x^2$ , find the value of  $k$

**[2 marks]**

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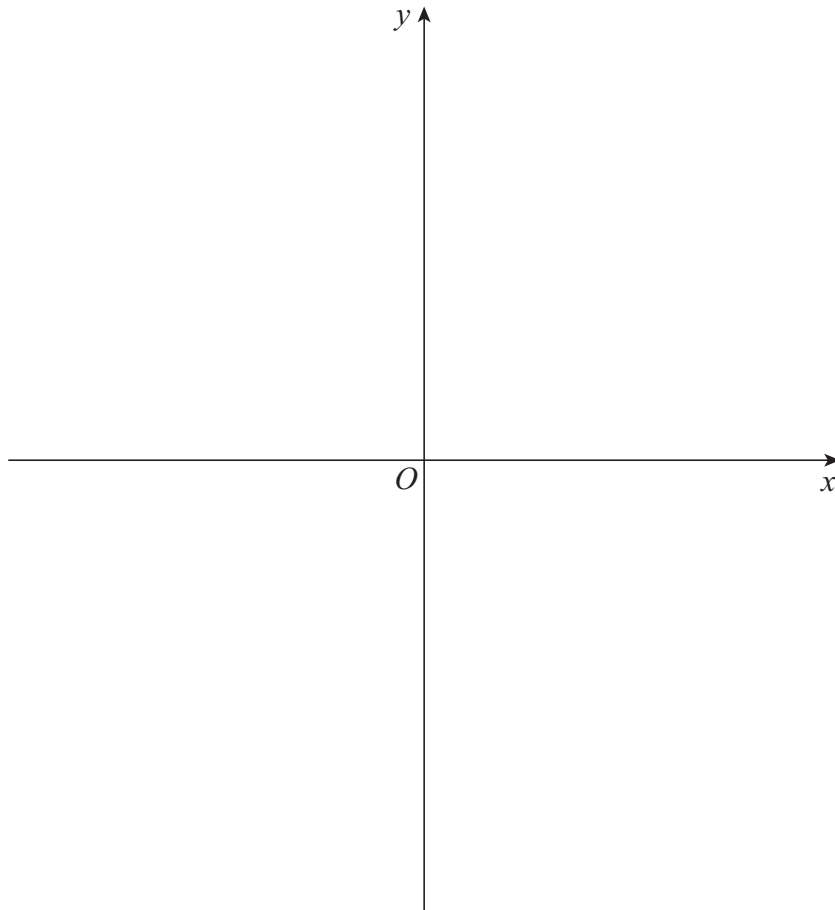
11 It is given that

$$f(x) = x(x - a)(x - 6)$$

where  $0 < a < 6$

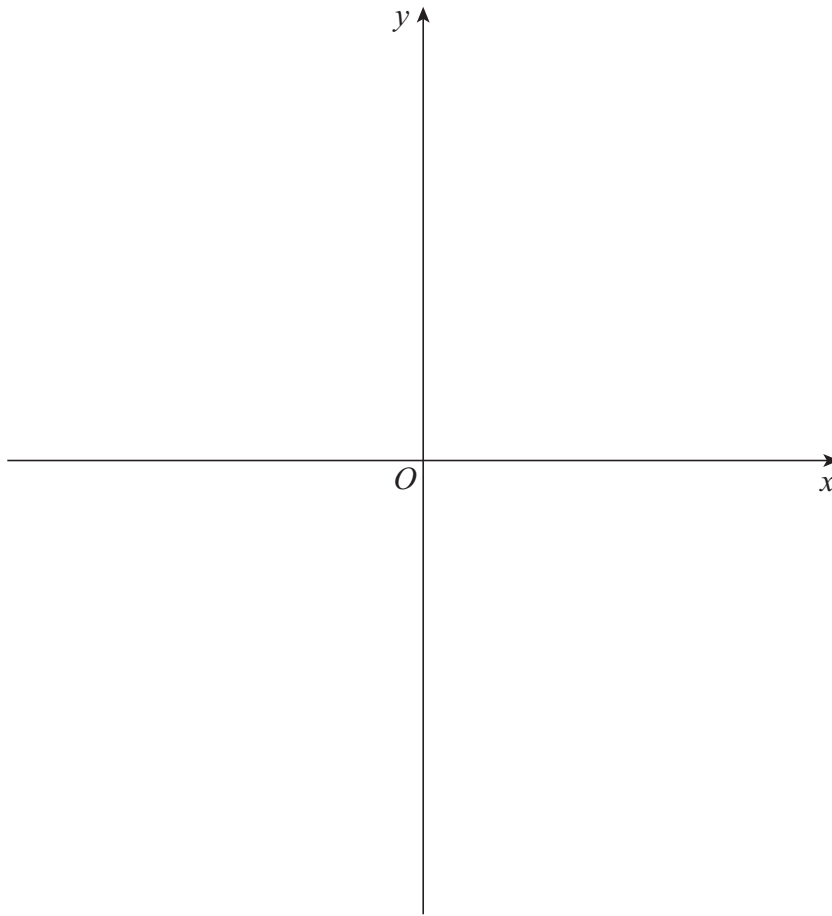
11 (a) Sketch the graph of  $y = f(x)$  on the axes below.

[3 marks]



**11 (b)** Sketch the graph of  $y = f(-2x)$  on the axes below.

**[2 marks]**



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**13 (a)** It is given that

$$P(x) = 4x^3 + 8x^2 + 11x + 4$$

Use the factor theorem to show that  $(2x + 1)$  is a factor of  $P(x)$

**[2 marks]**

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**13 (b)** Express  $P(x)$  in the form

$$P(x) = (2x + 1)(ax^2 + bx + c)$$

where  $a$ ,  $b$  and  $c$  are constants to be found.

**[2 marks]**

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**13 (c)** Given that  $n$  is a positive integer, use your answer to part **(b)** to explain why  $4n^3 + 8n^2 + 11n + 4$  is **never** prime.

**[2 marks]**

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14 (c) (ii) **Figure 1** below shows a sketch of parts of the graphs of

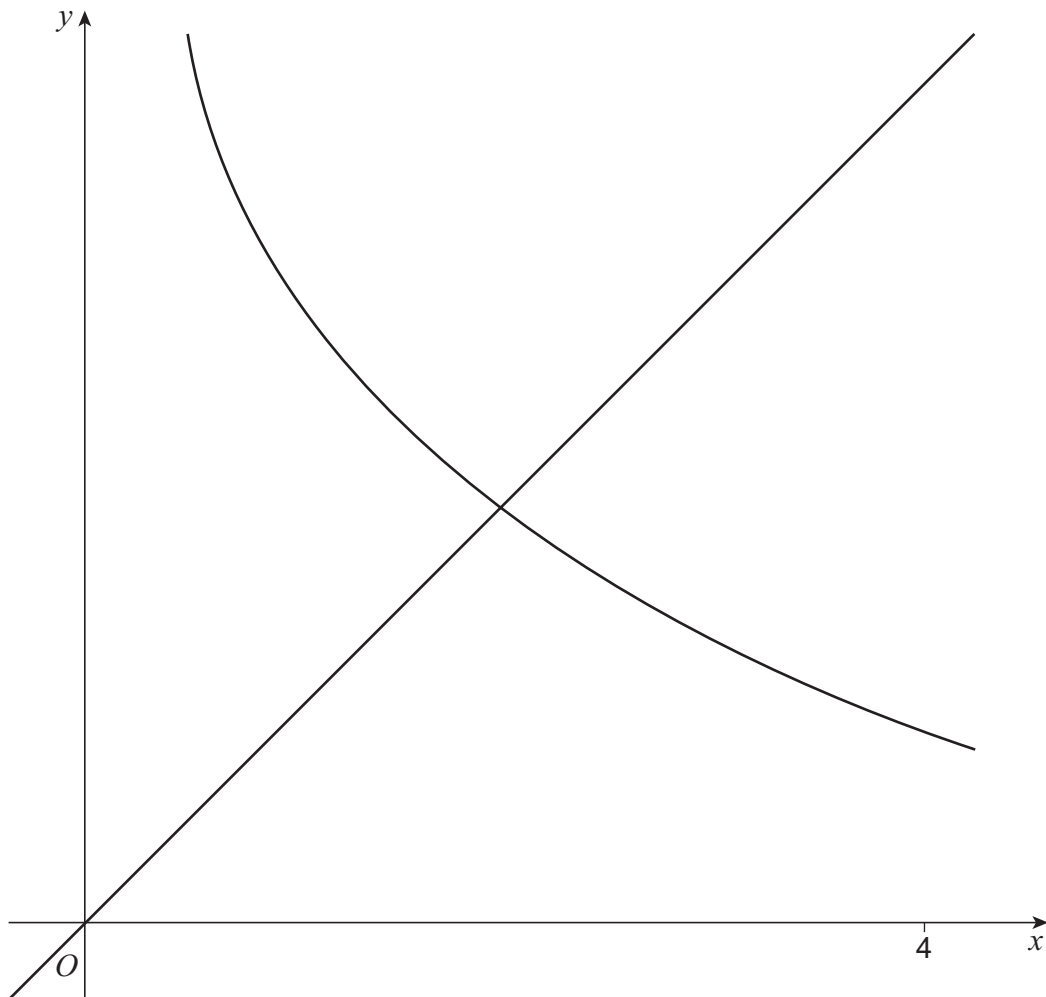
$$y = 3 - \frac{3}{2} \ln x \text{ and } y = x$$

On **Figure 1**, draw a staircase or cobweb diagram to show how convergence takes place.

Label, on the  $x$ -axis, the positions of  $x_2$ ,  $x_3$  and  $x_4$

**[2 marks]**

**Figure 1**



**14 (c) (iii)** Explain why the iterative formula

$$x_{n+1} = 3 - \frac{3}{2} \ln x_n$$

fails to converge to  $\alpha$  when the starting value is  $x_1 = 0$

**[1 mark]**

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**15 (b)** A student is attempting to solve the equation

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3 \text{ for } 0^\circ \leq \theta \leq 360^\circ$$

They use the result from part (a), and write the following **incorrect** solution:

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3$$

Step 1  $4 \cos \theta - \sec \theta = 3$

Step 2  $4 \cos \theta - \frac{1}{\cos \theta} - 3 = 0$

Step 3  $4 \cos^2 \theta - 3 \cos \theta - 1 = 0$

Step 4  $\cos \theta = 1$  or  $\cos \theta = -0.25$

Step 5  $\theta = 0^\circ, 104.5^\circ, 255.5^\circ, 360^\circ$

**15 (b) (i)** Explain why the student should reject one of their values for  $\cos \theta$  in Step 4.

[1 mark]

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**15 (b) (ii)** State the correct solutions to the equation

$$\sin 2\theta \operatorname{cosec} \theta + \cos 2\theta \sec \theta = 3 \text{ for } 0^\circ \leq \theta \leq 360^\circ$$

[1 mark]

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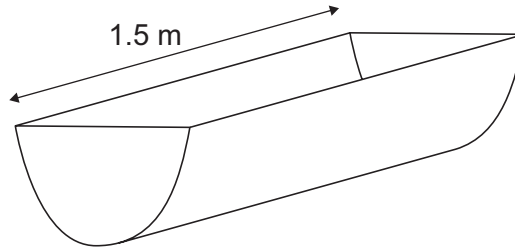
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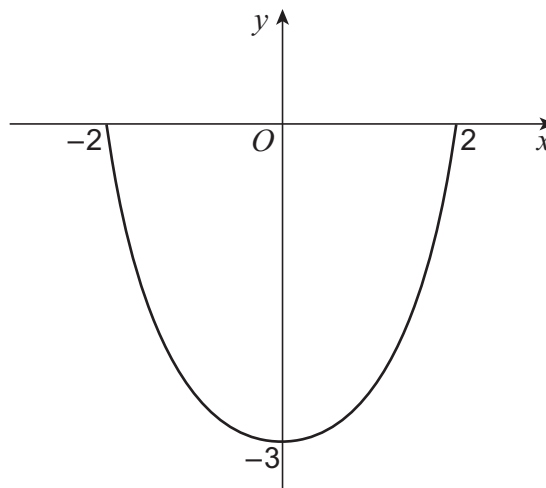
- 16 **Figure 2** below shows a 1.5 metre length of pipe.

**Figure 2**



The symmetrical cross-section of the pipe is shown below, in **Figure 3**, where  $x$  and  $y$  are measured in centimetres.

**Figure 3**





**17** The function  $f$  is defined by

$$f(x) = |x| + 1 \text{ for } x \in \mathbb{R}$$

The function  $g$  is defined by

$$g(x) = \ln x$$

where  $g$  has its greatest possible domain.

**17 (a)** Using set notation, state the range of  $f$

**[2 marks]**

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**17 (b)** State the domain of  $g$

**[1 mark]**

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**17 (c)** The composite function  $h$  is given by

$$h(x) = gf(x) \text{ for } x \in \mathbb{R}$$

**17 (c) (i)** Write down an expression for  $h(x)$  in terms of  $x$

**[1 mark]**

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**17 (c) (ii)** Determine if  $h$  has an inverse.

Fully justify your answer.

**[2 marks]**

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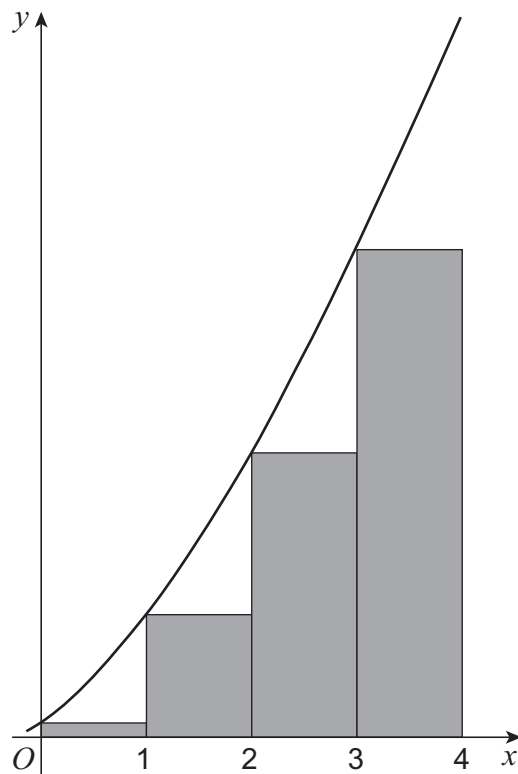
**18 (c)** A graph has the equation

$$y = (4x + 1)\sqrt{2x + 1}$$

A student uses four rectangles to approximate the area under the graph between the lines  $x = 0$  and  $x = 4$

The rectangles are all the same width.

All the rectangles are drawn under the curve as shown in the diagram below.















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